

EE215 – FUNDAMENTALS OF ELECTRICAL ENGINEERING

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WEEK 4 CIRCUIT ANALYSIS (II)

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MESH CURRENT ANALYSIS

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QUESTIONS TO ANSWER

- Mesh current analysis
 - How to establish mesh current equations for an electric circuit?
- Supermesh
 - What is a supermesh?
 - How to apply the technique to analyze an electric circuit?
- Source transformation
 - How to apply the technique to analyze an electric circuit?
- Superposition
 - How to apply the technique to analyze an electric circuit?

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MESH CURRENT METHOD (1)

- Def.: Mesh Current – a current that only exists in the perimeter of a mesh.
 - The mesh-current method is similar (“dual”) to the node-voltage method:

Node Voltage Method	Mesh Current Method

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MESH CURRENT METHOD (2)

- Write KVL for every mesh in terms of *mesh currents*.
- What's a *mesh*? A loop that does not contain any other loops within it.
- In essence, every "window" in a planar circuit is a mesh.
- *Mesh current* is current that flows in the mesh.
- Branches have either one or two mesh currents flowing through them. If two, they usually flow in opposite directions.

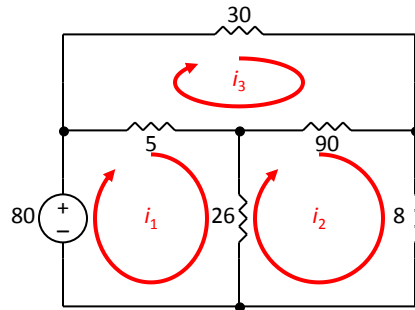
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EXAMPLE

- Mesh 1:
- Mesh 2:
- Mesh 3:

Multiplying out the terms:



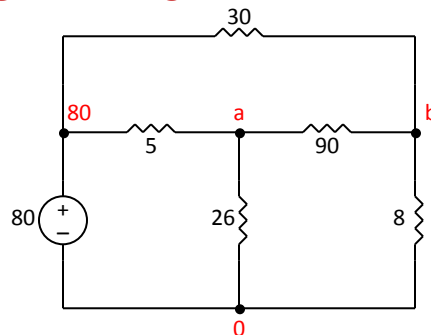
Solving this system yields

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COMPARE WITH NODE VOLTAGE METHOD

- Node a:
- Node b:



- Solving this system yields
- In this example, node voltage method is more efficient than mesh current method. **Why?**

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SUPERMESHES

- Two neighboring meshes that “share” a current source can be combined into a “supermesh”.
- Principle:

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MESH CURRENT METHOD

- Example (with dependent current source)

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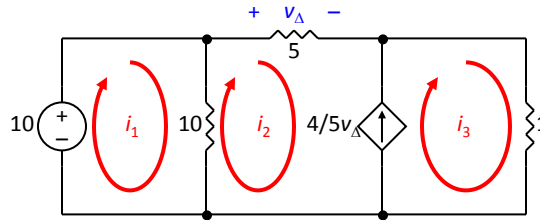
- Supermesh:

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MESH CURRENT METHOD

- Example (with dependent current source)



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SOURCE TRANSFORMATION

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SOURCE TRANSFORMS (1)

... another technique to simplify circuits

- Def.: Equivalence –

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SOURCE TRANSFORMS (2)

- Example

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SOURCE TRANSFORMS (3)

- Example

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SOURCE TRANSFORMS (4)

- Example

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SOURCE TRANSFORMS (5)

- Example

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SOURCE TRANSFORMS (6)

- Example

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SOURCE TRANSFORMS (7)

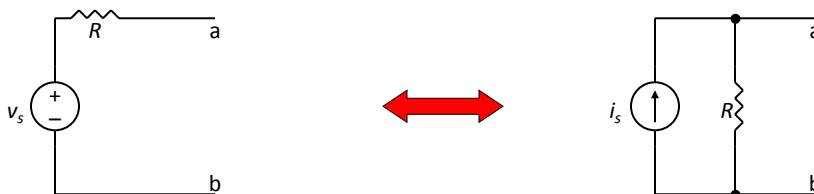
- Example

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SOURCE TRANSFORMS (8)

Equivalent circuits:



- Condition:

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SOURCE TRANSFORMS (9)

- What if there is a resistor R_p parallel to v_s , or a resistor R_s in series to i_s ?

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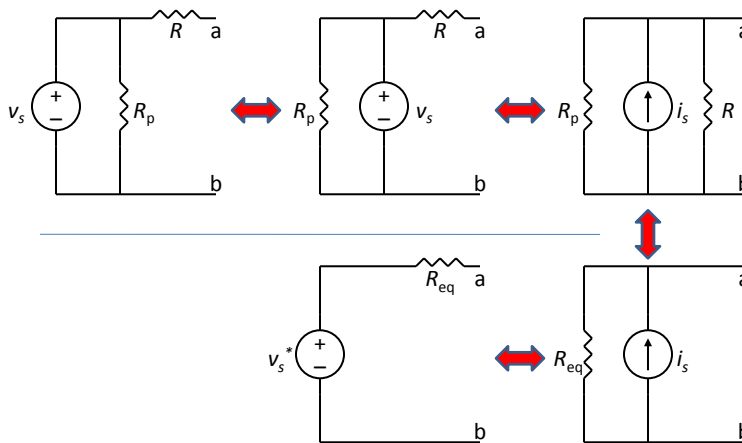
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SOURCE TRANSFORMS (10)

- What is wrong with this series of transforms?



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SOURCE TRANSFORMS (11)

- Example: $R = R_p = R_L$ in first and last circuit

- Source transforms cannot be done at arbitrary locations in the circuit

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SUPERPOSITION

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SUPERPOSITION (1)

- Example: Circuit 1

- Circuit 2

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SUPERPOSITION (2)

- Example: Circuit 3

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SUPERPOSITION (3)

- Circuit 1 is like Circuit 3 with current source switched off (current $i_0 = 0$).
- Circuit 2 is like Circuit 3 with voltage source switched off (voltage drop $v_0 = 0$).
- Effects of v_0 and i_0 are independent; they can be added (or superimposed).
- Reason: resistive circuits are linear systems.